

# Physics-Based Modeling for Total Ionizing Dose Effects

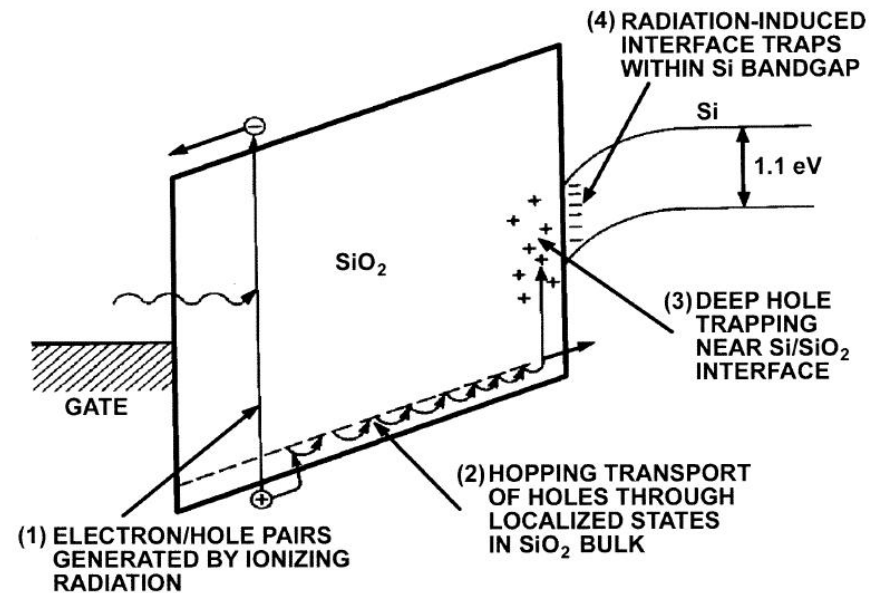
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Cogenda Co. Ltd, Suzhou, China  
2016-06-28

# Outline

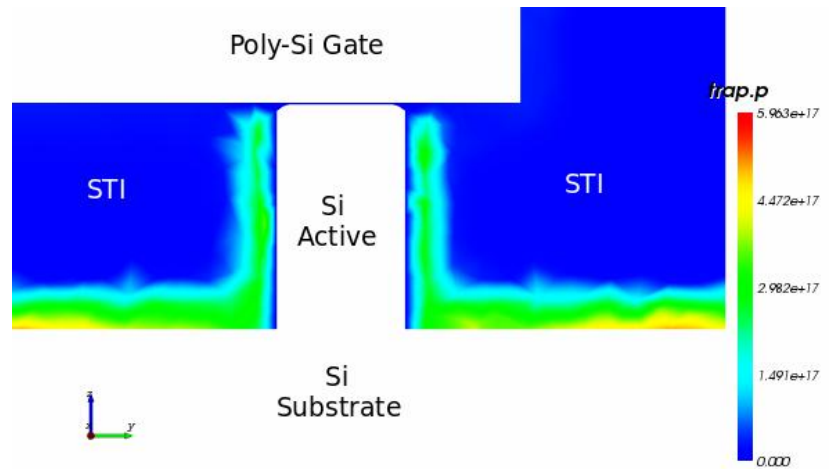
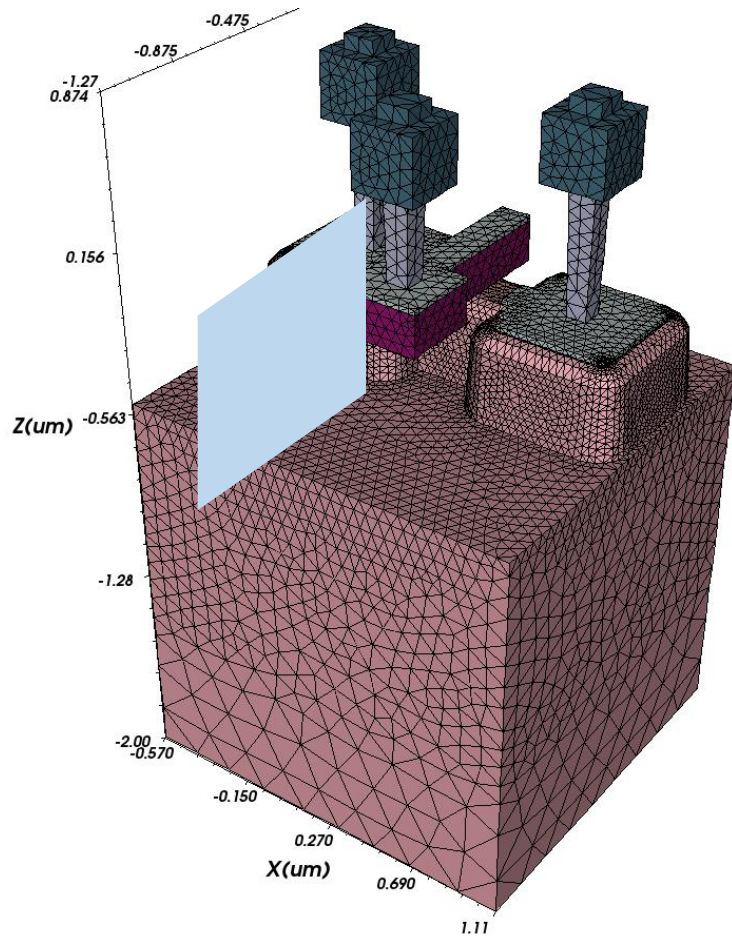
- Background
  - Total Ionizing Dose Effects in CMOS
- Physics-based TCAD Simulation
  - Governing Equations
  - Solver Implementation
  - Results
- Physics-based Compact Modeling
  - Motivation
  - Core Equations
  - Results

# Physical Mechanism of TID: Consensus

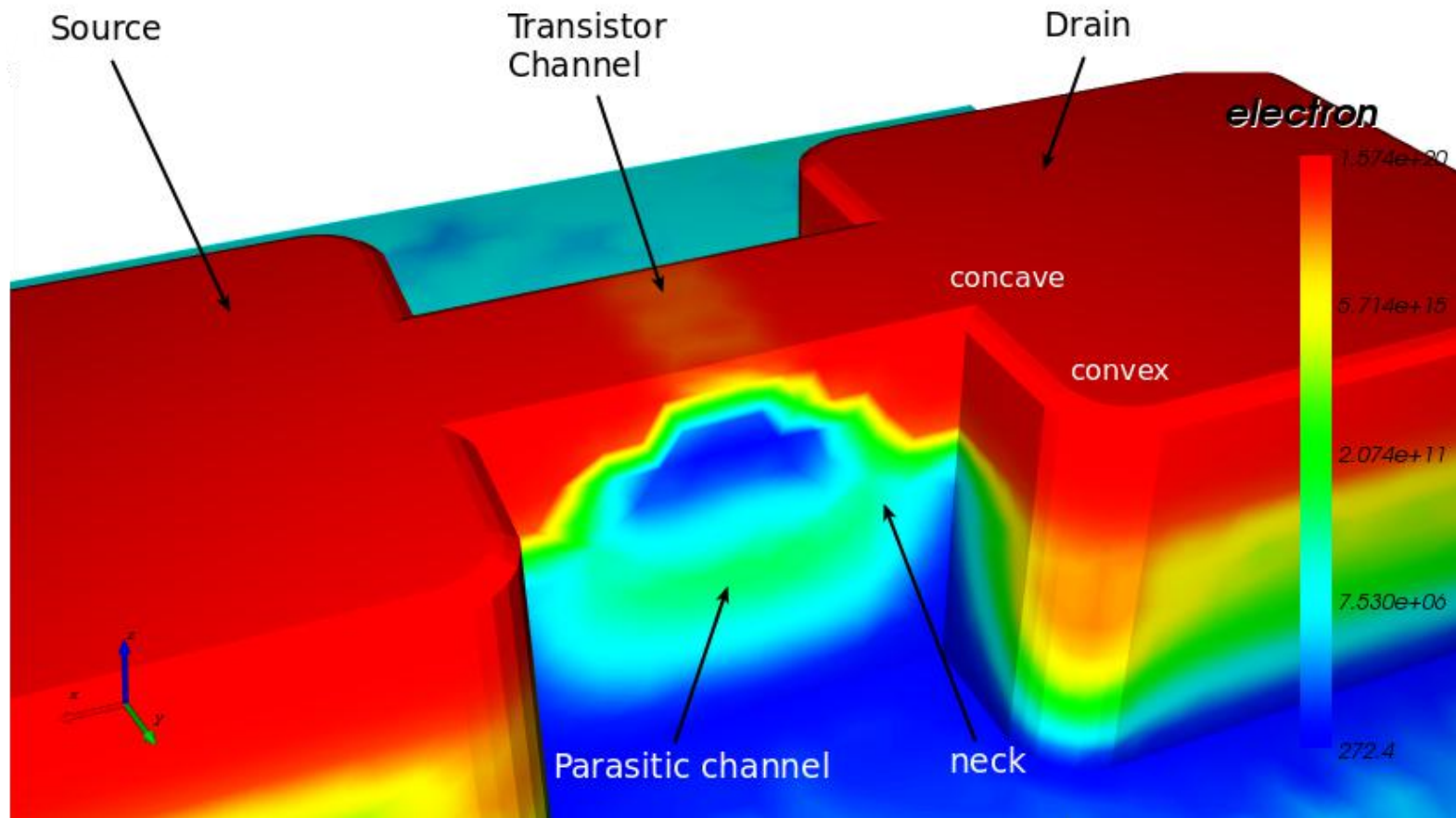
- Ionizing radiation  $\rightarrow$  e/h pairs
- e/h pairs recombine unless separated by E-field
- $e^-$  swept out quickly
- $h^+$  hopping slowly
- $E'$  centers capture holes (trapped charge)



# Trapped Charge Build-up in Oxide



# TID-Induced Parasitic Channel



# Physics and Governing Equations

Ionization:

$$G_{rad} = Y(E) \cdot g_0 \cdot \dot{D}$$
$$Y(E) = \left( \frac{E}{E + 1.35 \times 10^6 \text{V/cm}} \right)^{0.9} \quad \text{for X ray}$$
$$Y(E) = \left( \frac{E}{E + 0.55 \times 10^6 \text{V/cm}} \right)^{0.7} \quad \text{for } \gamma \text{ ray}$$

Electrostatics: ....

Transport of mobile species: ....

Reactions: ....

# Physics and Governing Equations

Electrostatics

$$\nabla \epsilon \nabla \psi = -\frac{1}{e}(p + T_p - n)$$

Transport of mobile species

Electron

$$\frac{dn}{dt} = \nabla \cdot (\mu_n n E + D_n \nabla n) + G_n - R_n$$

Hole

$$\frac{dp}{dt} = -\nabla \cdot (\mu_p p E - D_p \nabla p) + G_p - R_p$$

H<sup>+</sup>

$$\frac{dH^+}{dt} = -\nabla \cdot (\mu_{H^+} H^+ E - D_{H^+} \nabla H^+) + G_{H^+} - R_{H^+}$$

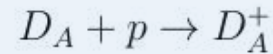
Reactions:

....

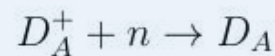
# Physics and Governing Equations

Reactions:

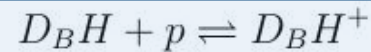
hole capture at  $D_A$



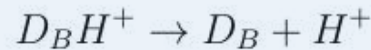
electron capture at  $D_A$



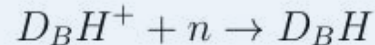
hole capture/emission at  $D_B$



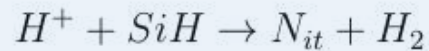
H+ release from  $D_B$



electron capture from  $D_B$



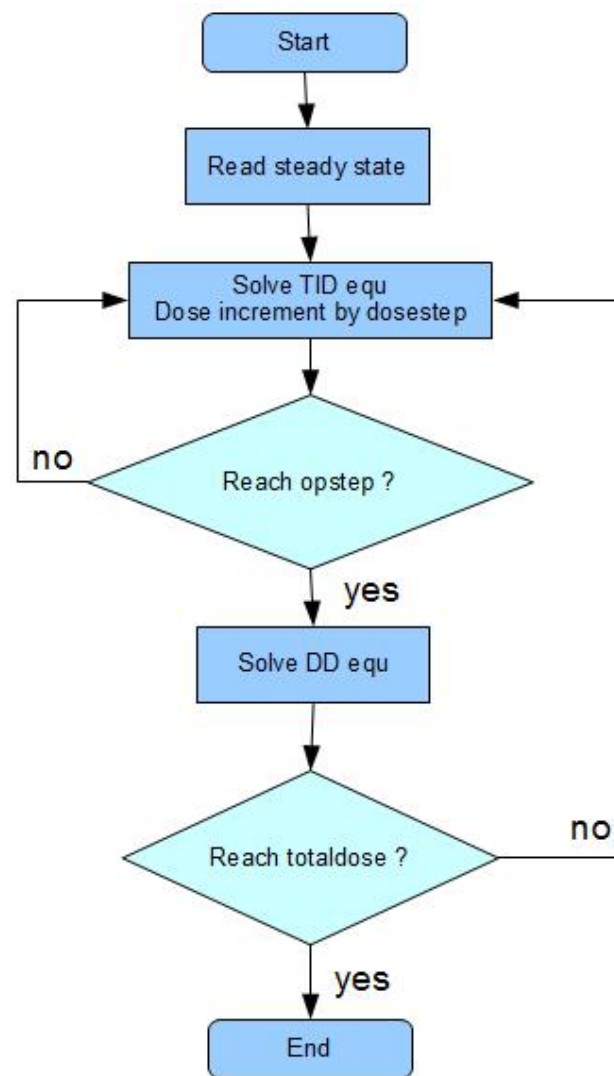
Interface trap production



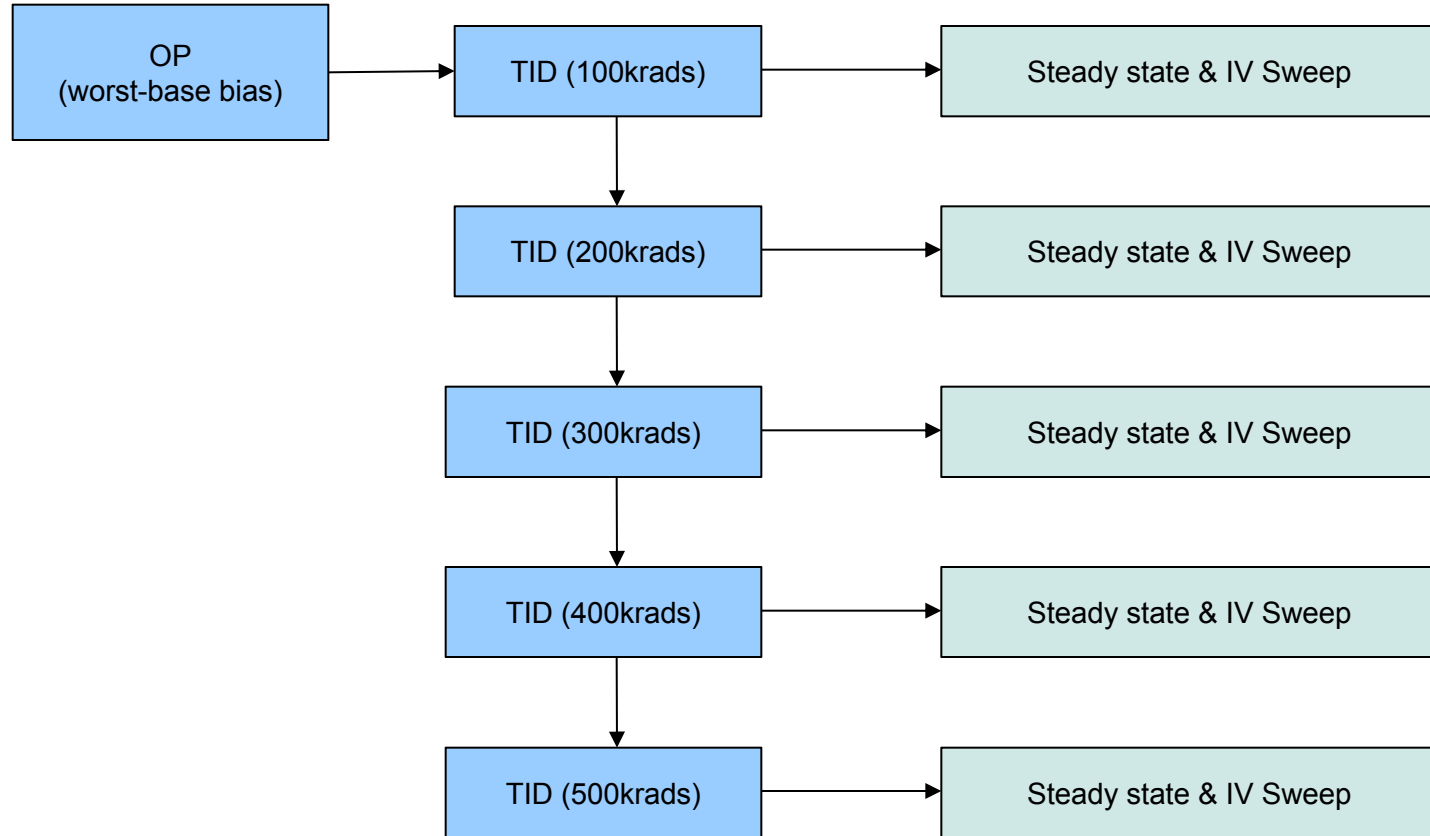


# Numerical Implimentation

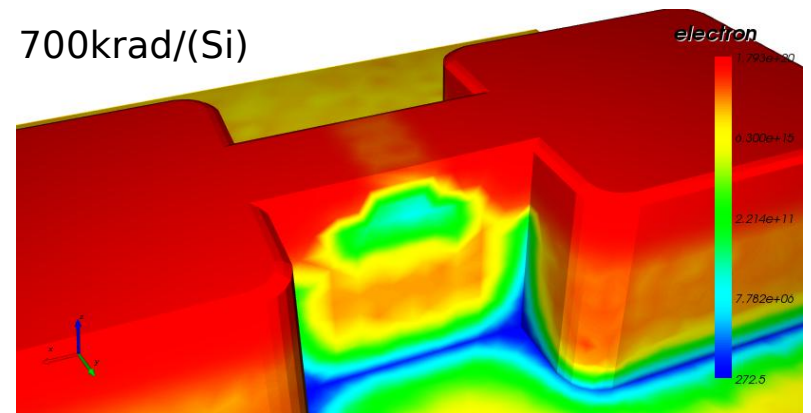
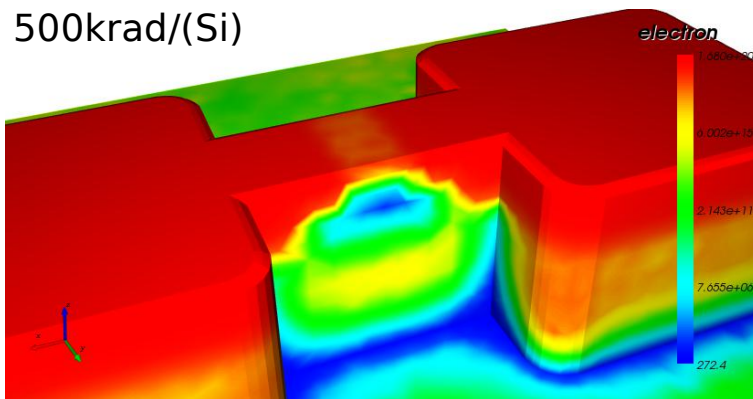
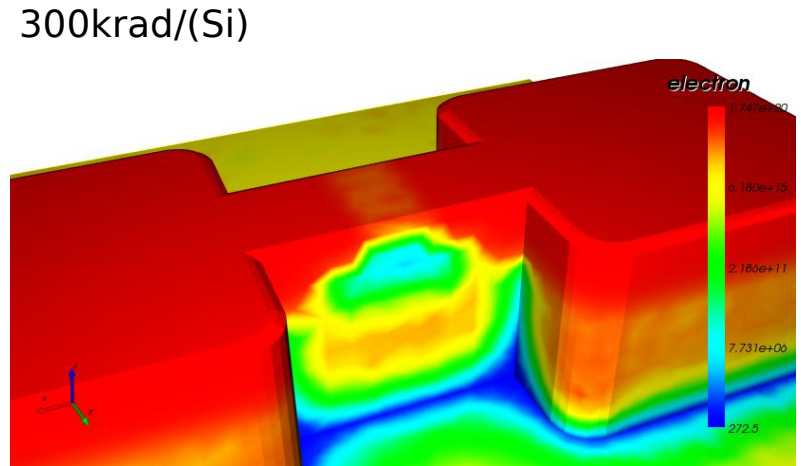
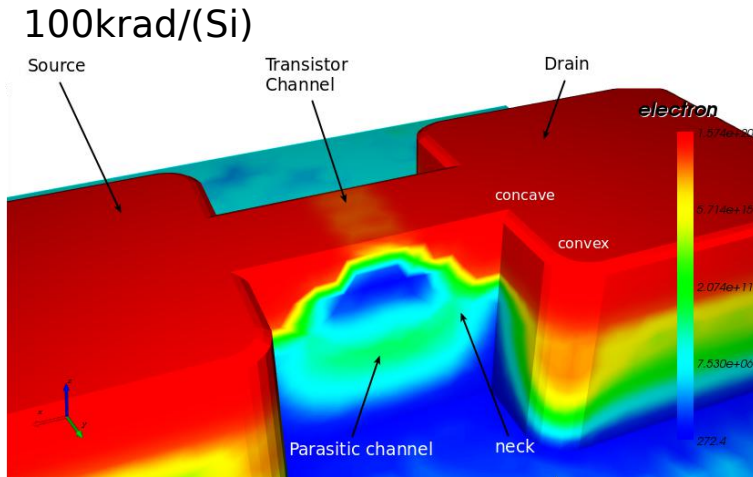
- 3D TID solver in Genius
  - TID effect slowly disturb the potential in silicon region
    - Only solve TID equations on silicon oxide, while
    - keeps potential constant at silicon/metal regions
  - Do global potential update every ~3K Rad
  - This makes the TID solver stable and fast



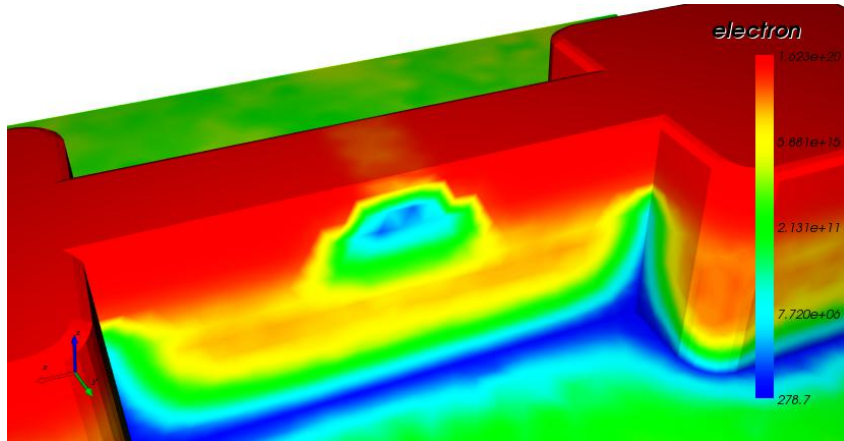
# TID Simulation Flow



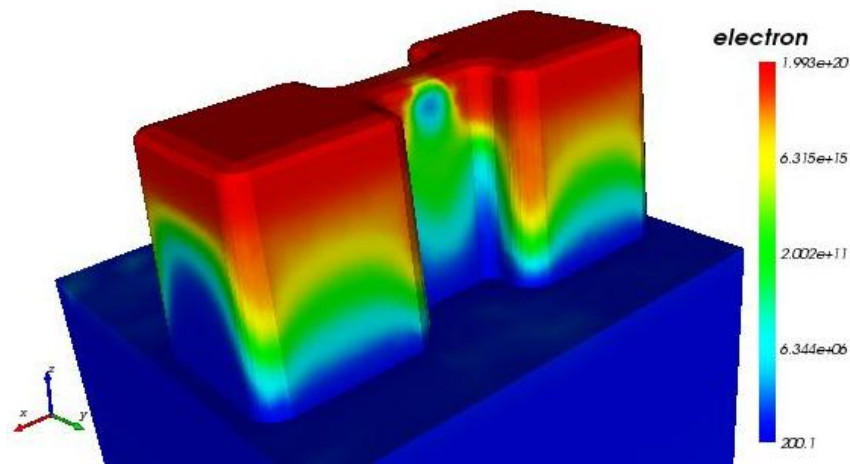
# Parasitic Channel due to TID



# Parasitic Channel due to TID

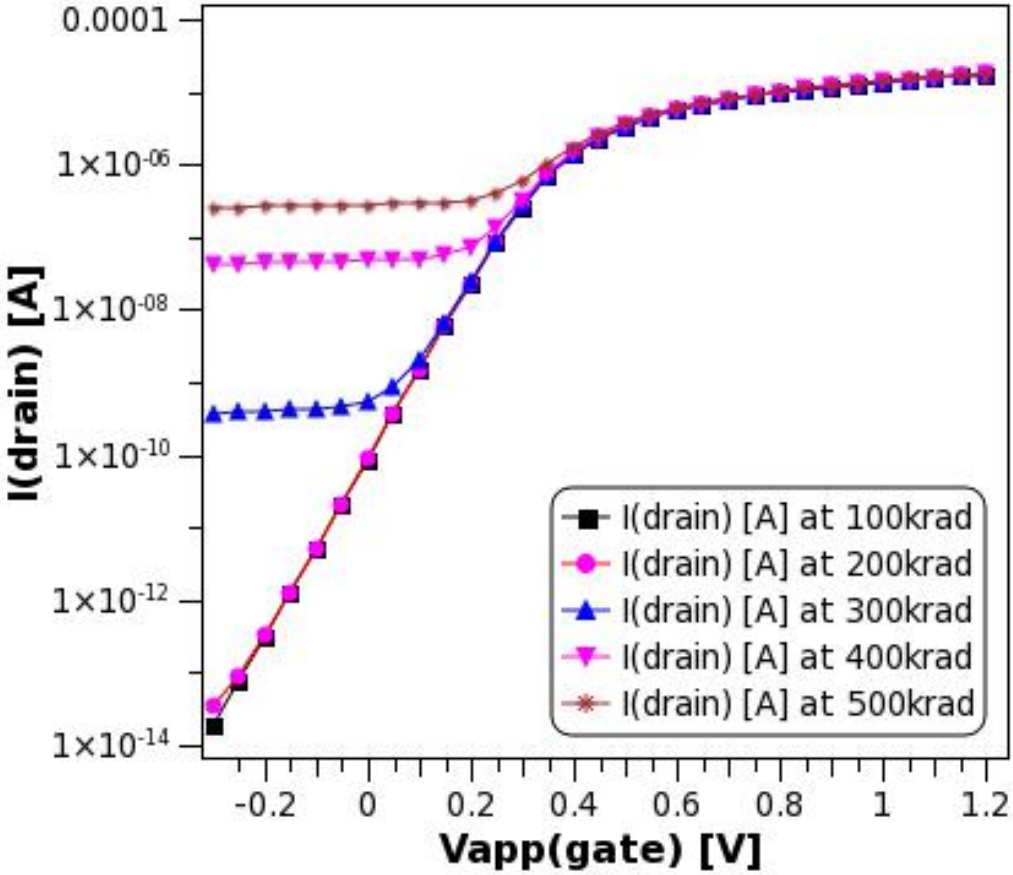


- 0.13um, another layout



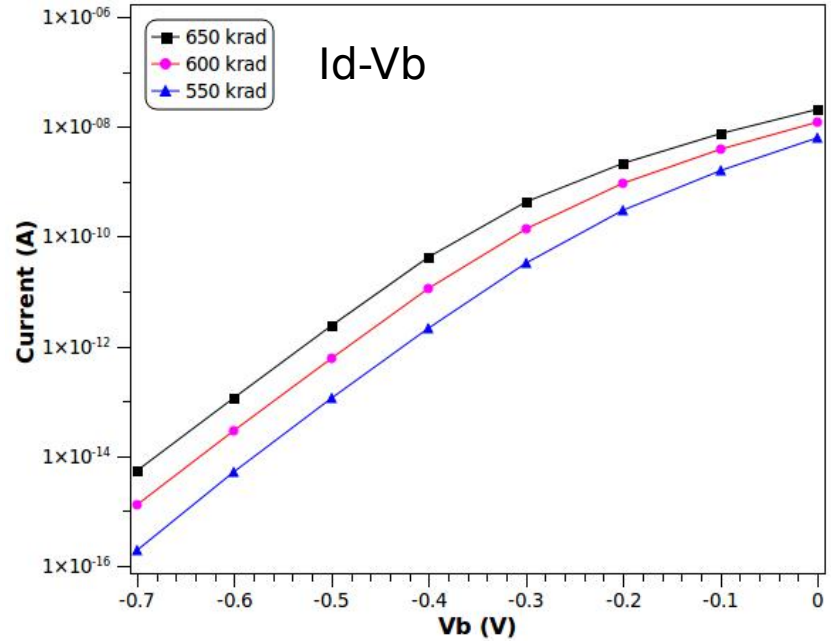
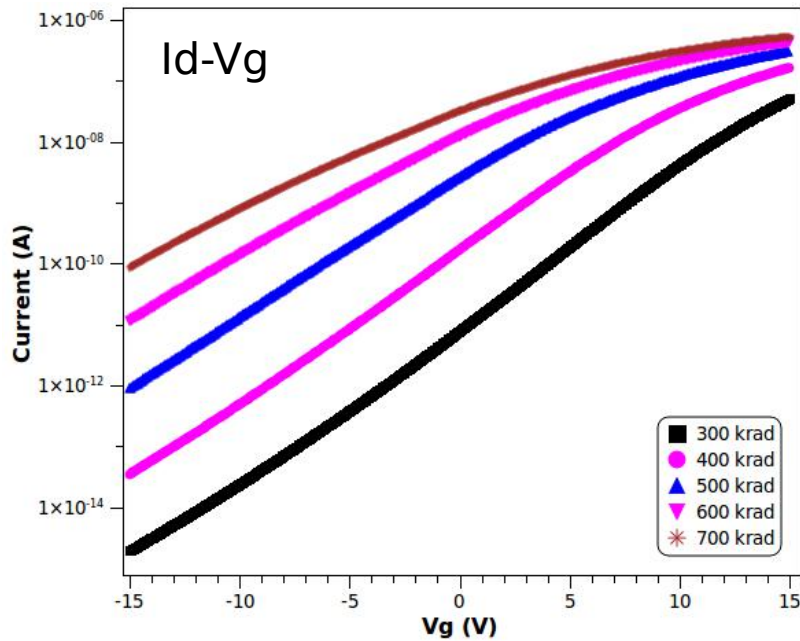
- 65nm, nMOSFET

# Simulated IV Curves due to TID



# IV Curves of Sidewall Parasitic Tr

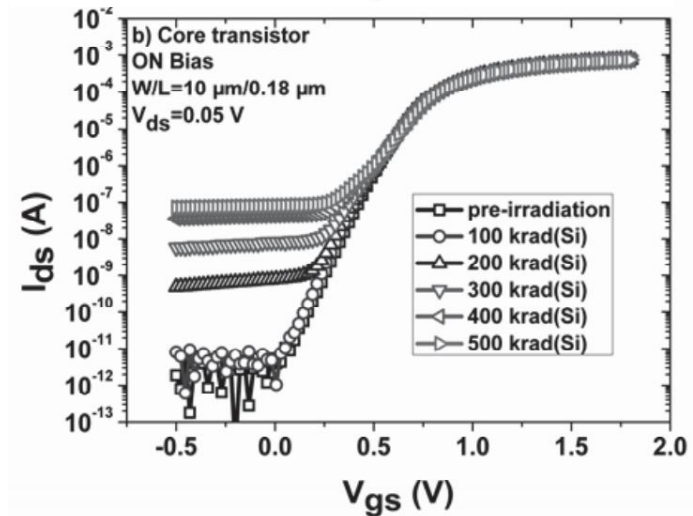
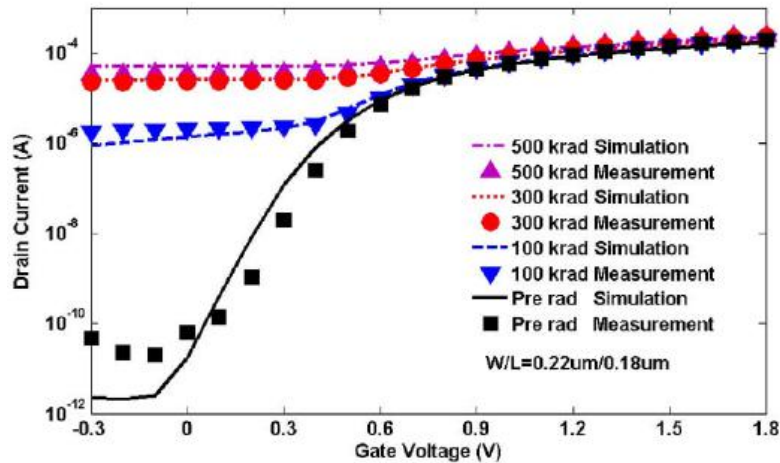
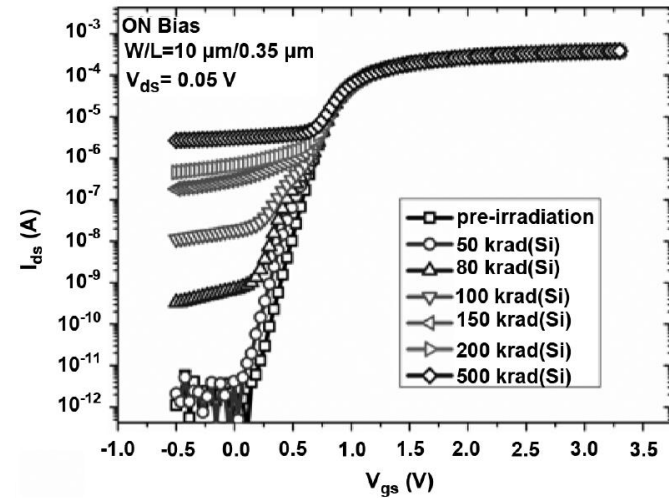
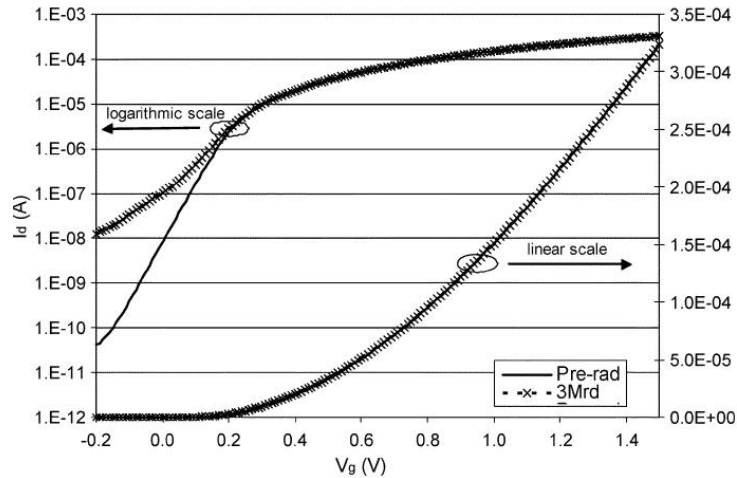
Separate parasitic from intrinsic MOSFET



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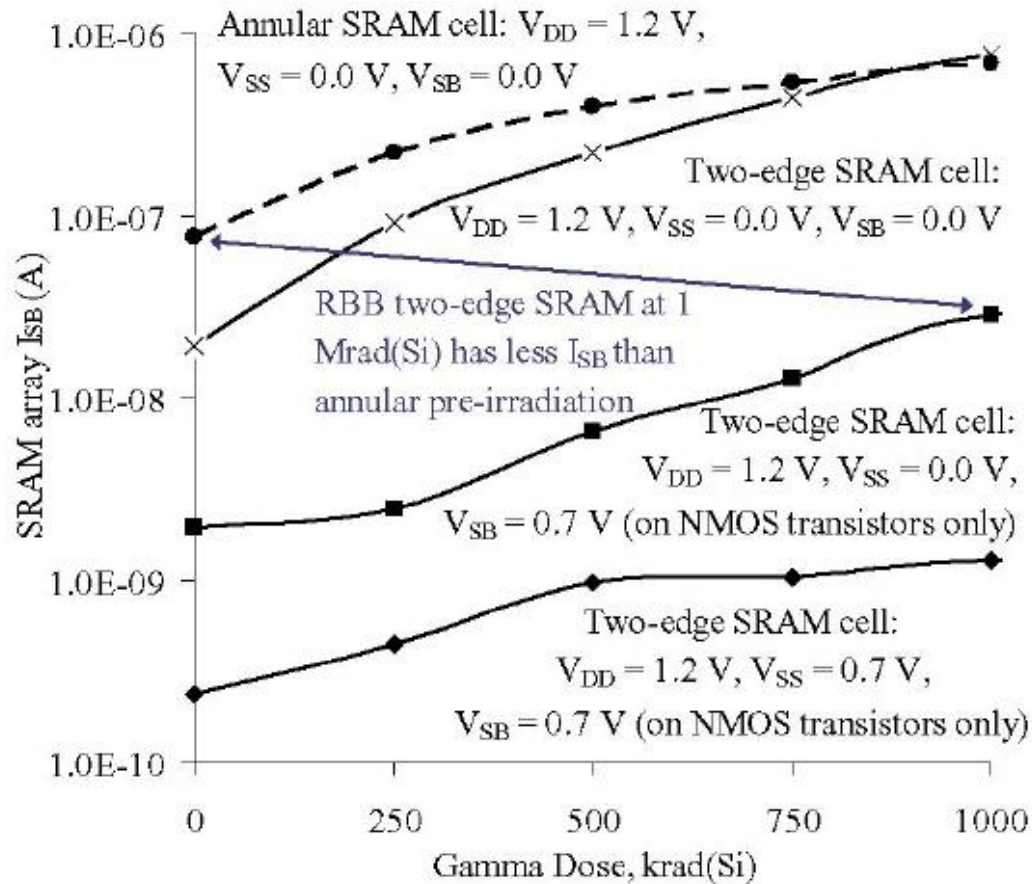
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# TID in CMOS: Experiment Data





# Motivation: Why Substrate Bias?

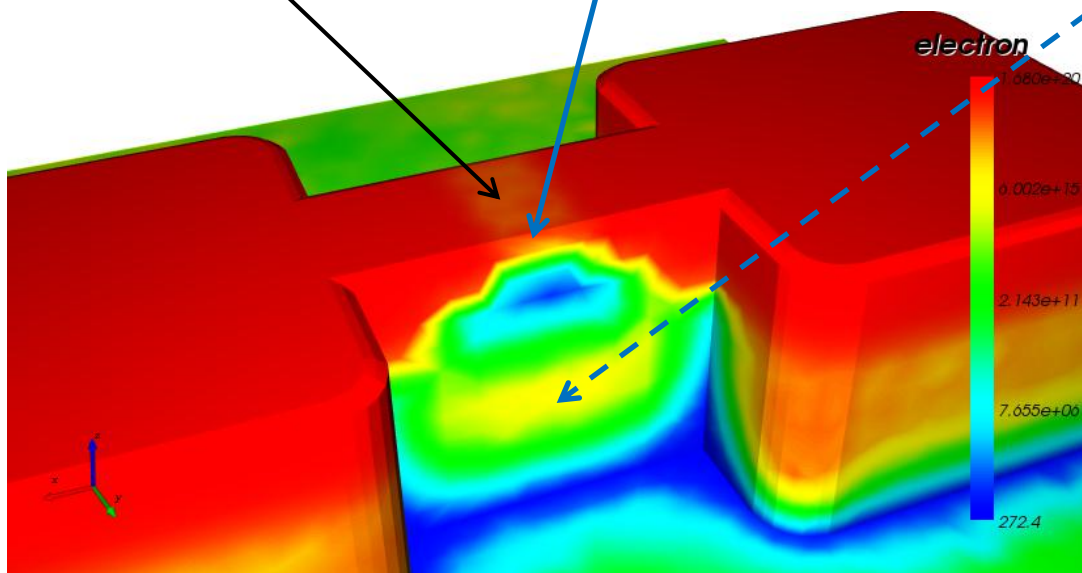


# TID-Induced Parasitic Channel

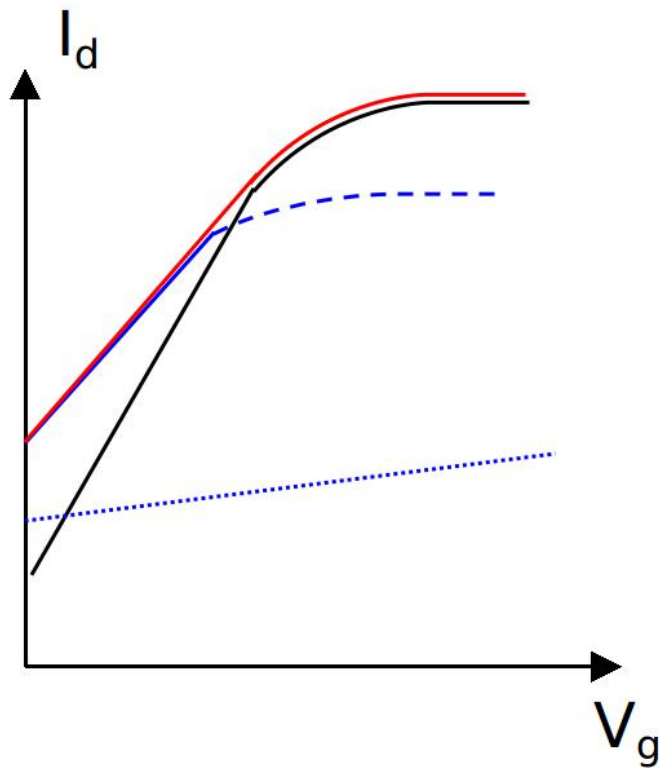
Intrinsic MOSFET

Corner Parasitic MOSFET

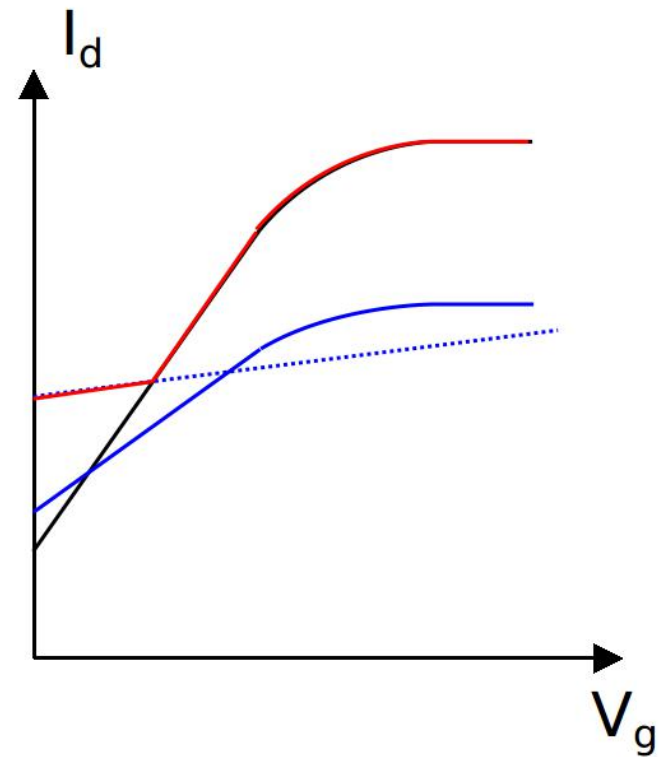
Sidewall Parasitic MOSFET



# TID in CMOS: Mechanism



corner parasitic  
MOSFET dominates



sidewall parasitic  
MOSFET dominates

# Sub-threshold IV of Parasitic Transistor

sub-threshold IV

$$I_{ds} = \mu \frac{W}{L} V_T^2 C_{dep} \exp \frac{V_{gs} - V_{th}}{\kappa V_T} \exp \frac{V_{bs}}{\eta V_T} \left( 1 - e^{-\frac{V_{ds}}{V_T}} \right)$$

Vg dependence

Vb dependence

threshold voltage and fixed charge

$$V_{th} = V_{fb} - \frac{Q_D}{C_{ox}} + 2\phi_b \left( 1 + \frac{C_{dep}}{C_{ox}} \right)$$

$$Q_D = 1.2 \times 10^{11} \text{ cm}^{-2} \times q_0 \times \left( \frac{D_D}{100 \text{ krad}} \right)^{0.65}$$

# Model Synthesis: IV

smoothing function: sub-threshold to above threshold

$$Q_{\text{inv}} = \frac{2C_{\text{ox}}\kappa V_T \cdot \ln \left[ 1 + \exp \left( \frac{V_{\text{gs}} - V_{\text{th}}}{2\kappa V_T} \right) \right]}{1 + 2\kappa \frac{C_{\text{ox}}}{C_{\text{dep}}} \exp \left( -\frac{V_{\text{gs}} - V_{\text{th}} - 2V_{\text{off}}}{2\kappa V_T} \right) \exp \left( \frac{-V_{\text{bs}}^\gamma}{\eta \times V_T} \right)}$$

Main IV equation:

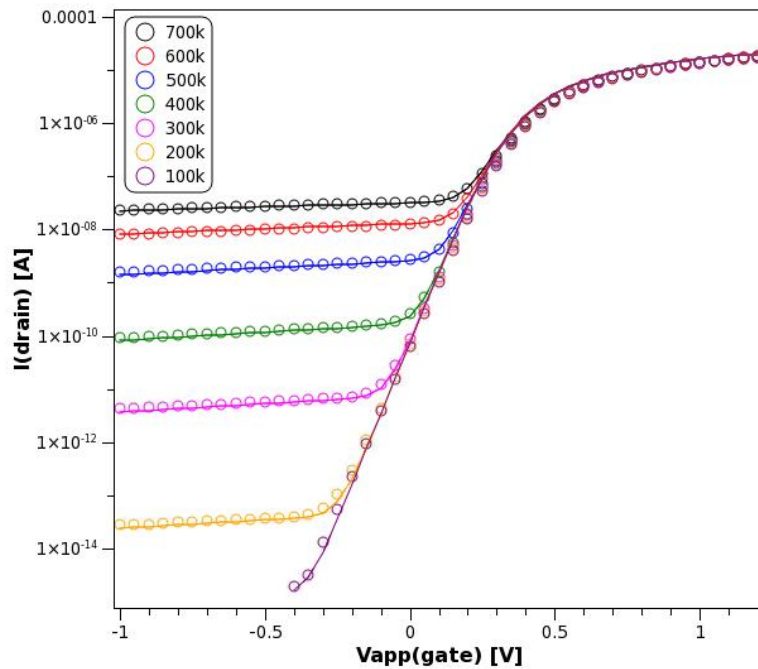
$$I_{\text{ds}} = \mu V_T Q_{\text{inv}} \cdot \left[ 1 - \exp \left( -\frac{V_{\text{ds}}}{V_T} \right) \right] \cdot \left( \frac{Z}{L} \right)_{\text{eff}} \cdot f_W$$

W and L dependence

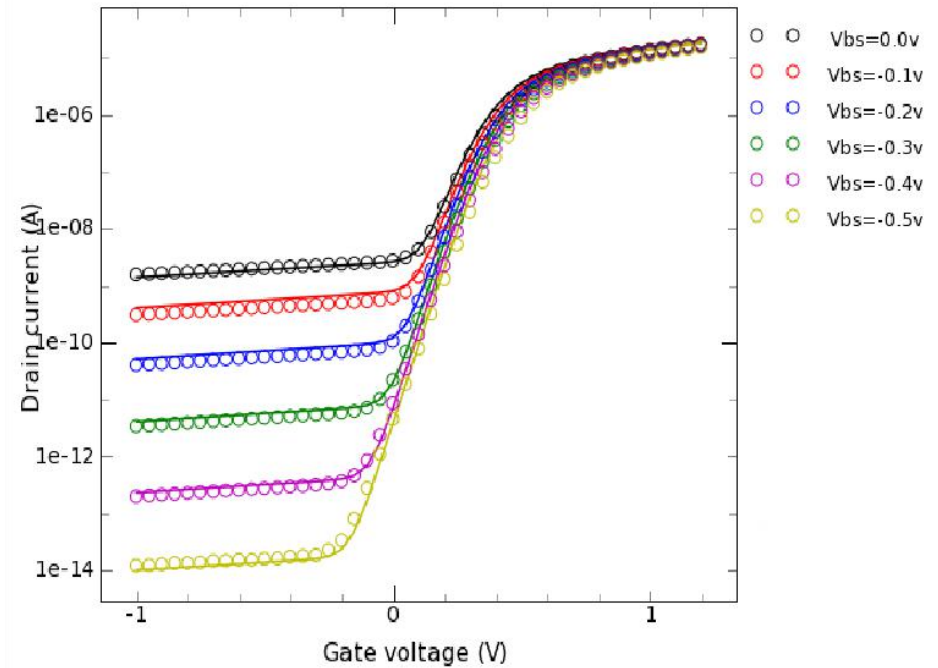
$$\left( \frac{Z}{L} \right)_{\text{eff}} = Z_{\text{eff}} \cdot \frac{(L_{\text{min}} + L_{\text{ref}})}{(L + L_{\text{ref}}) \cdot L_{\text{min}}}$$
$$f_W = (A_W \times W^{B_W} + C_W)$$

# Simulation Results

## Compact Model vs TCAD



dose dependence



$V_{\text{b}}$  dependence

# Summary

- Physics-Based Modeling of TID Effects
  - TCAD level
    - First 3D solver for TID effects
    - Not and Nit in oxide
    - Parasitic channel in MOSFET due to TID
    - Separate contribution from parasitic channels
  - Compact model level
    - Guided by TCAD simulation of parasitic IV
    - Models the V<sub>bs</sub> dependence of leakage current
    - Implemented as subcircuit macro