

A field solvers view on constructing compact models for devices in an electromagnetic ambient

Wim Schoenmaker – MAGWEL

Nick van der Meijs – TU Delft

Daniel Ioan – Polytechnical University Bucharest

- Introduction
- Field solvers
- Field solver view on devices
- Ambient effects
- Devices and EM ambient
- Conclusions

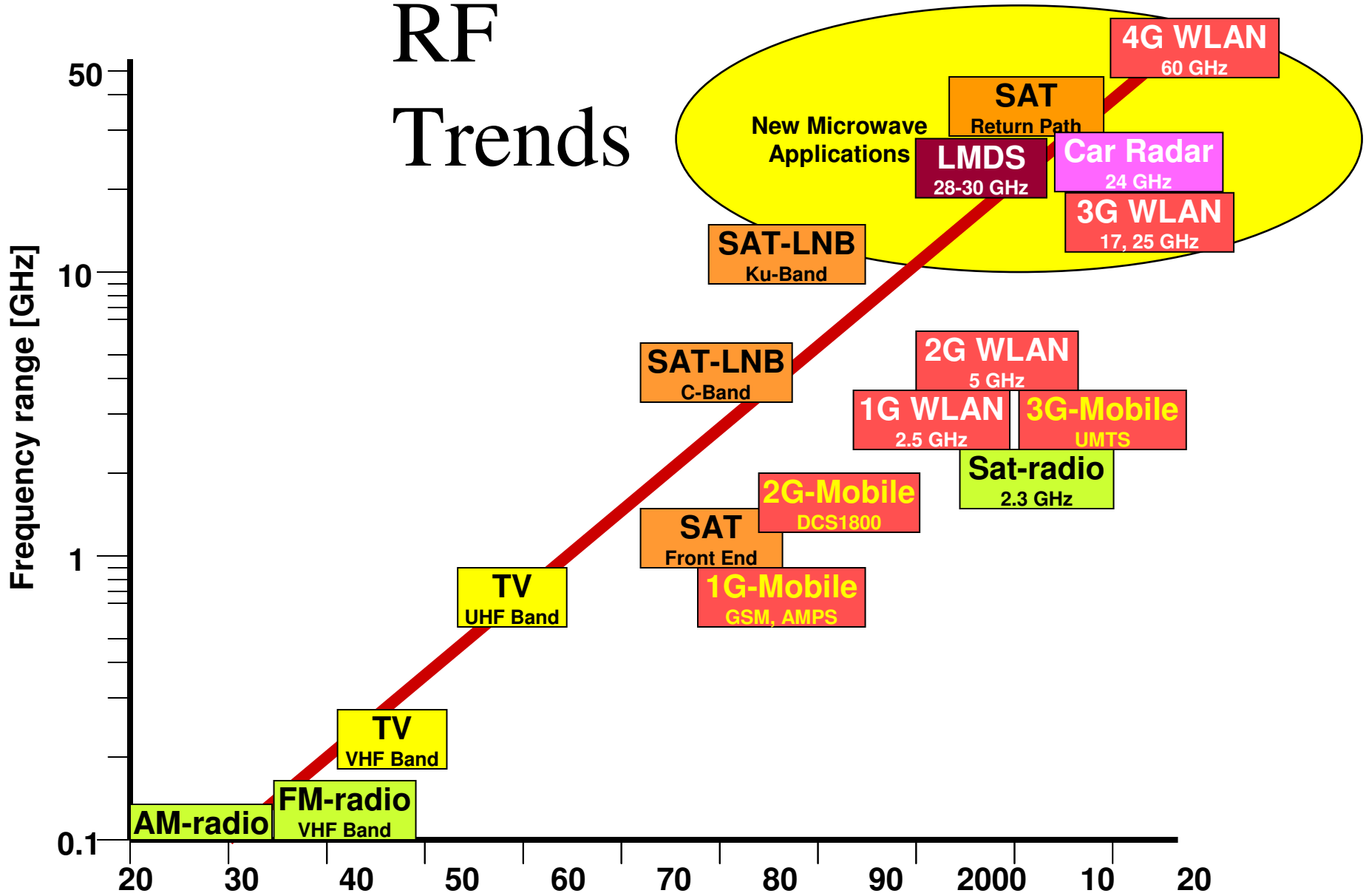
Introduction

- After the RF applications now the μ -wave and mm-wave applications will be integrated on silicon
- CMOS will start dominating in RF and will slowly take up in μ /mm-wave applications and so trigger here also the integration trend
- EM tools are needed to understand/analyze the complex behavior of circuits, especially where Kirchhoff's laws will start deviating from reality

Courtesy: Dominique Leenaerts (PHILIPS)

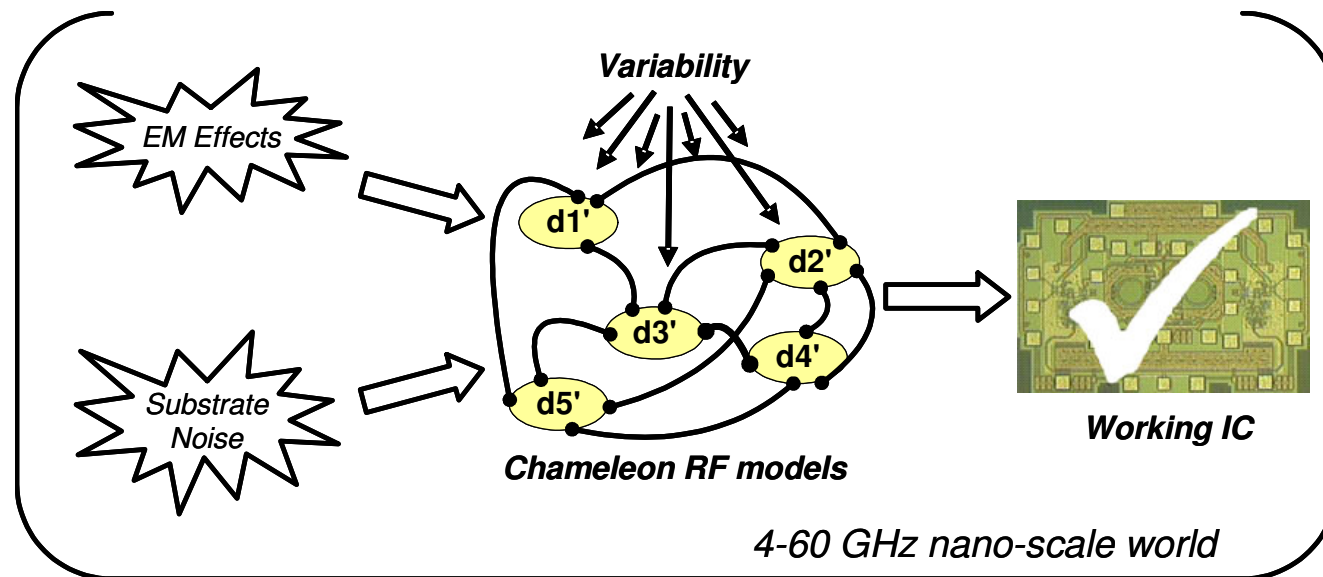
Introduction

RF Trends



Introduction

- CHAMELEON-RF EU project
- device characterisation and environment influences
- tools for a thorough and accurate post-design verification



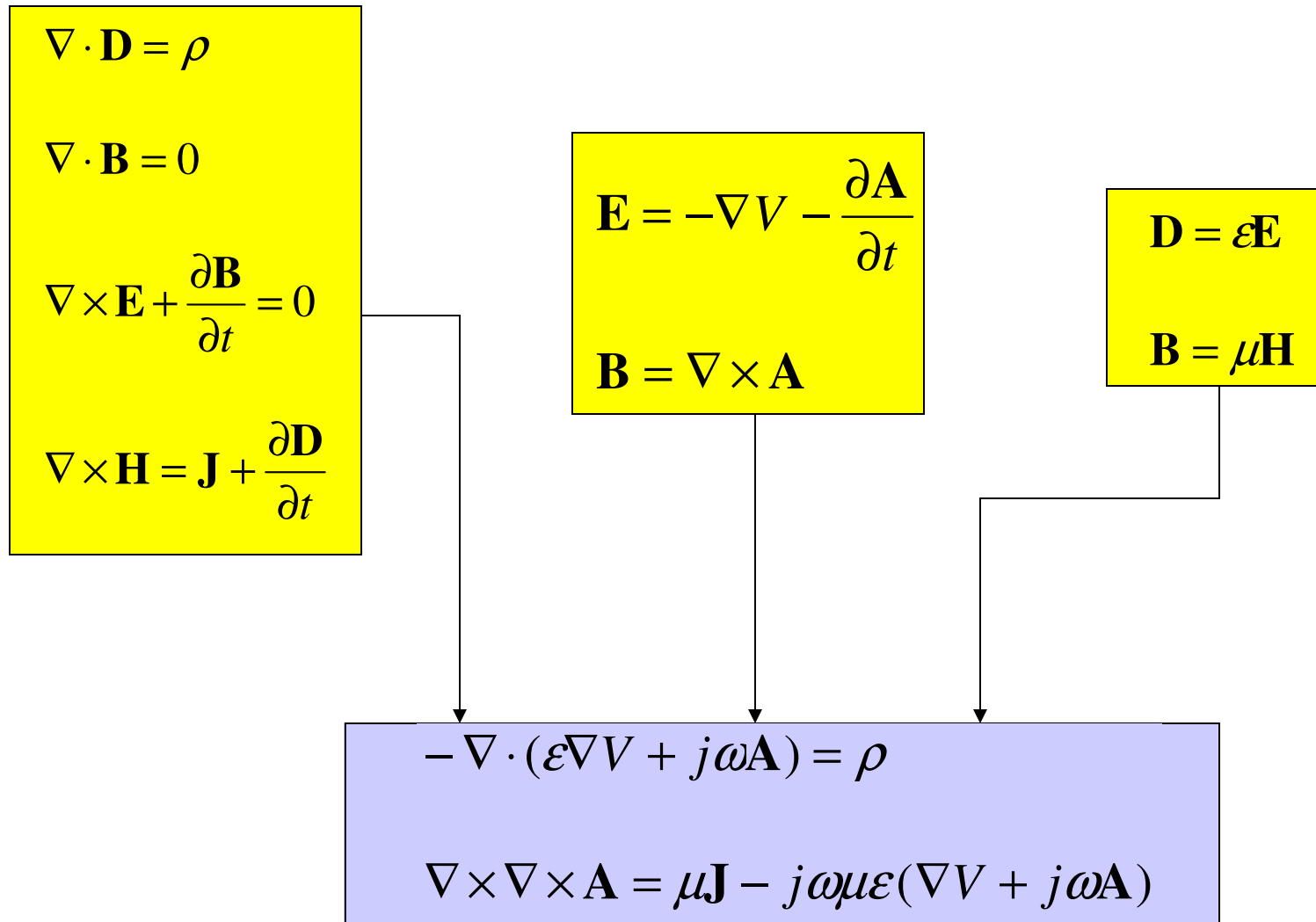
- **CHAMELEON-RF work flow**

- electromagnetic field aspects of coupling, at the component level.
- coupling of the front-end (active devices) with back-end
- refinement of compact models will be refined with ‘hooks’ or connectors that allow the incorporation of induced field effects
- Reduced-order modelling (ROM) of the SPICE net lists
- Inclusion of variability in the ROM
- Design, processing, characterization of test devices
- Validation

- Example: Effects of integrated passives on transistors
- Problem definition:
 - *Integrated passive component inject high-frequency electric fields into active devices.*
- Open issue:
 - *How does this modify the operation of the active devices ?*
- Use field solvers to address this problem

Architecture:

- Start from the ‘fundamental’ equations of physics
 - Maxwell equations
 - Drift-diffusion equation (or variation thereof)
 - Ohm’s law
 - Models for the material parameters
- Output
 - Current and voltages at contacts
 - S-parameters
 - ‘Inside looks’ e.g. field intensities, current densities



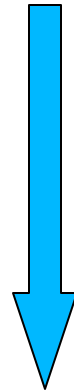
- Connection with Kirchhoff's laws through V variables

Semi-conductors

Conductors

$$\nabla \cdot \mathbf{j} = -j\omega\rho$$

$$\mathbf{j} = \sigma \mathbf{E}$$



$$\nabla \cdot \mathbf{j}_n - q j\omega n = U(n, p)$$

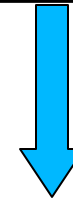
$$\nabla \cdot \mathbf{j}_p + q j\omega p = -U(n, p)$$

$$\rho = q(p - n + N_D - N_A)$$

$$\mathbf{j}_n = q\mu_n n\mathbf{E} + kT\mu_n \nabla n$$

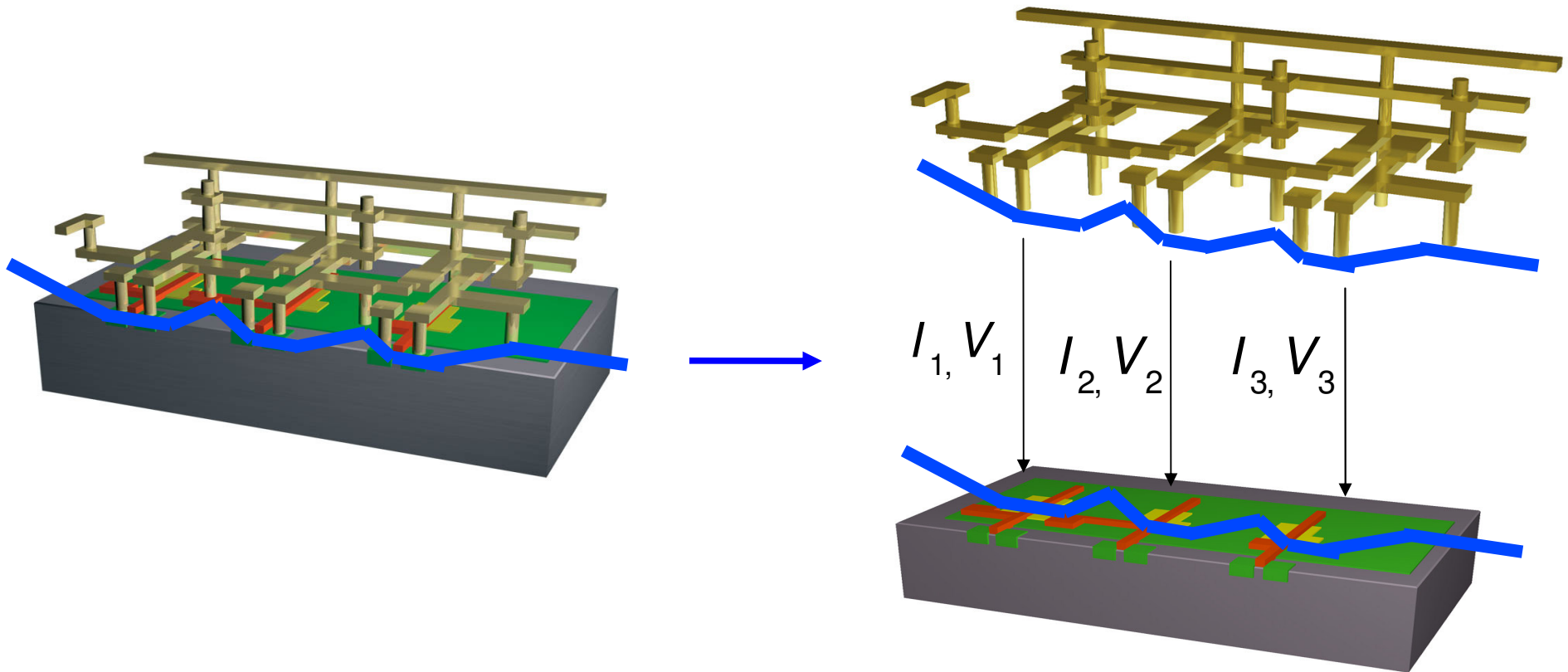
$$\mathbf{j}_p = q\mu_p p\mathbf{E} - kT\mu_p \nabla p$$

$$\mathbf{j} = \mathbf{j}_n + \mathbf{j}_p$$



- Back-end ('on' silicon) and Front-end ('in' silicon) issues can now be addressed in one environment

Decoupled in- and on-Silicon simulation



Reduce interaction between in- and on-Silicon part to currents and voltages at contacts. And use a different simulator for each part.

Some considerations

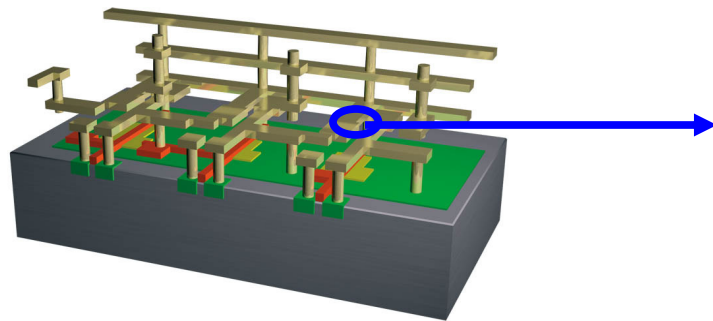
- At high frequencies: $|\nabla V| \approx |\omega \mathbf{A}|$
- Skin effect: $\mathbf{E} \approx 0$ because both terms cancel
- Serious induction \mathbf{E} -fields are injected
- These fields are superimposed on the \mathbf{E} - fields of the contact bias conditions
- Electromagnetic TCAD studies structures under ‘RF’ conditions

Some considerations

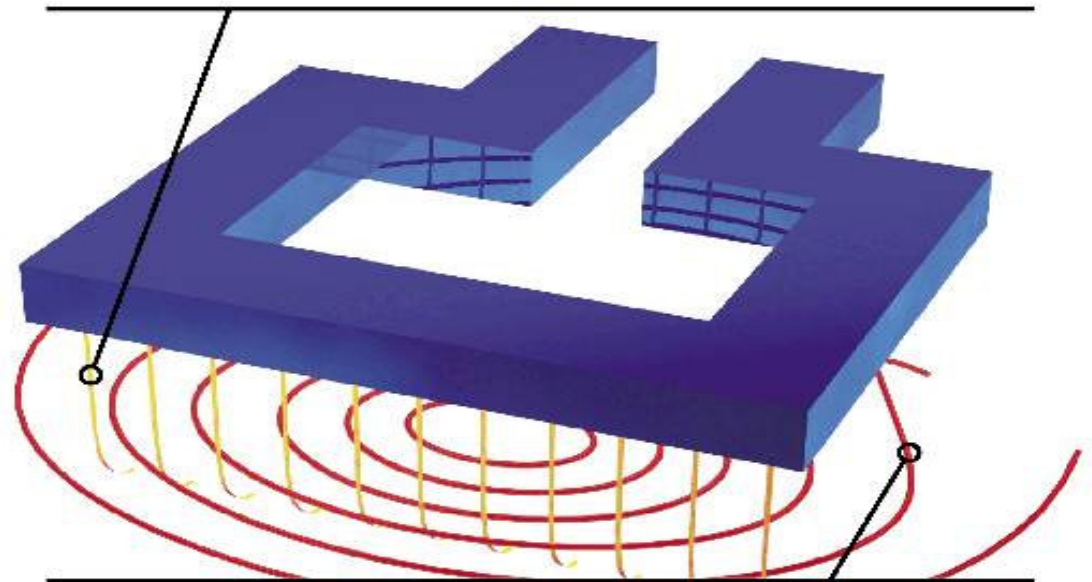
The link with Kirchhoff:

- Currents(In) = Current(Out)
 - This is not evident for finite-element implementations
 - Finite-volume integration implementations respect this requirements (MAGWEL)
- *Three* kinds of materials are encountered in a simulation set-up
 - Highly non-trivial interface conditions!

Two types of EM effects



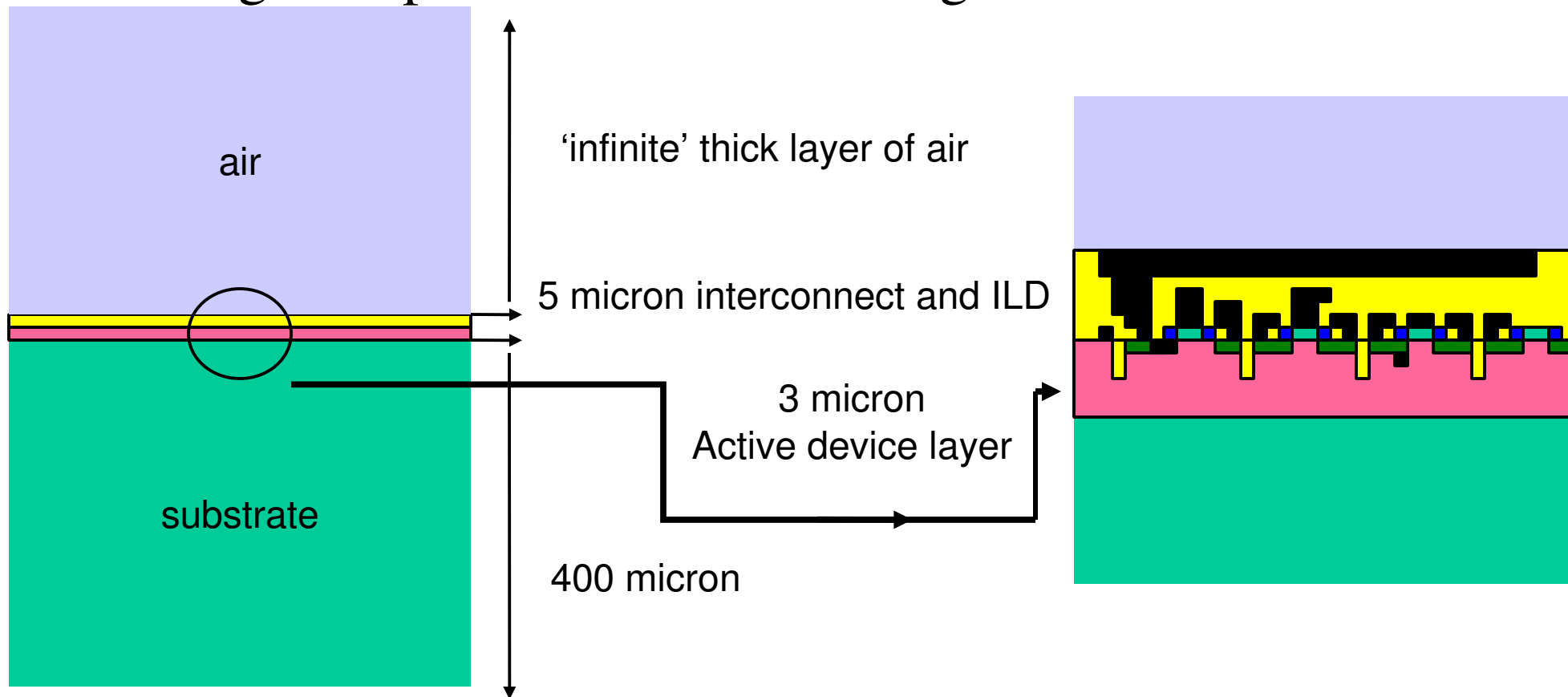
Electrically induced currents
in semiconductor substrates



Magnetically induced drift and
displacement currents in
semiconductor substrates

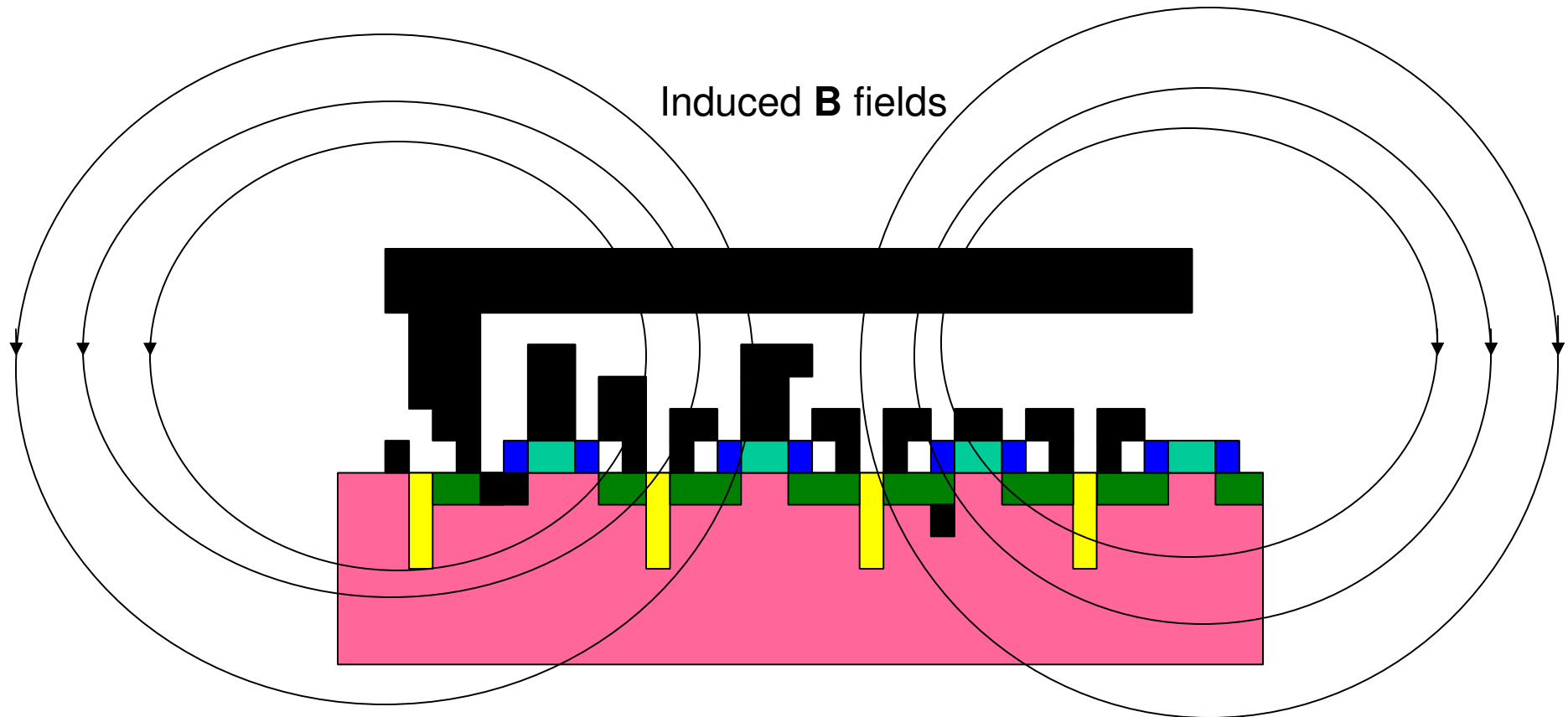
Active and passive structures

- Situation of the problem
 - Different scales under consideration
 - Integrated passive devices \gg single active devices



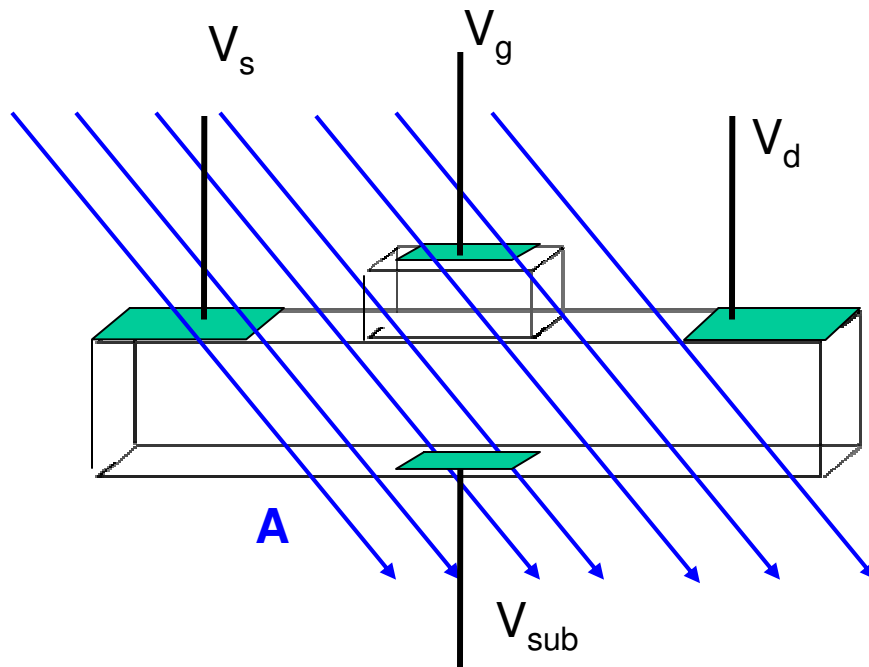
Field solver's approach

- The passive device injects a vector potential in the active device of which the magnitude and director can be taken *constant* over the device dimensions

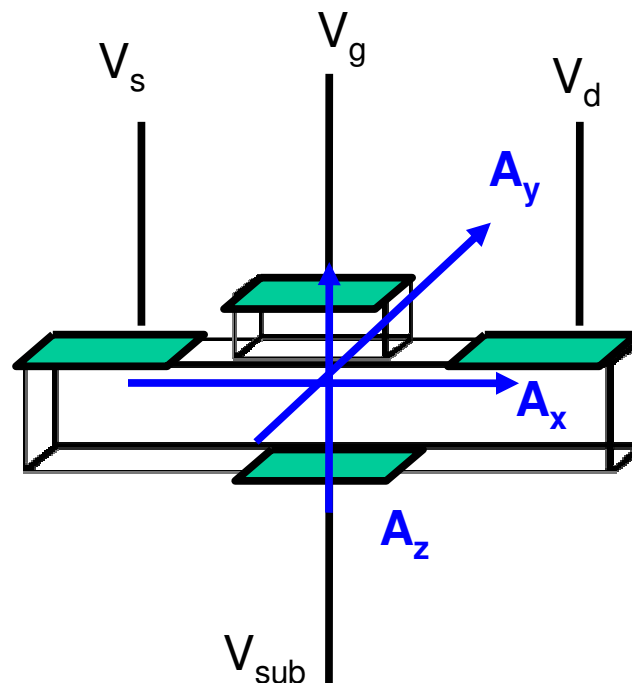


Field solver's approach

- A transistor now senses also an external \mathbf{A} vector
- RF Transistor modeling
 - Voltages at the gate, source, drain and substrate
 - External vector field through the transistor
 - Electric field in the transistor: $\mathbf{E} = -\nabla V - j\omega \mathbf{A}$



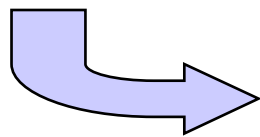
- The **A** field has 3 components:
 - A_x changes $V_{ds} : V_{ds} \rightarrow V_{ds} + j\omega\mathbf{A} \cdot \Delta\mathbf{x} = V_{ds}^{eff}$
 - A_z changes $V_{g,sub} : V_{g,sub} \rightarrow V_{g,sub} + j\omega\mathbf{A} \cdot \Delta\mathbf{z} = V_{g,sub}^{eff}$
 - The vector potential moves the transistor state in the IV plots
 - Move fully imaginary



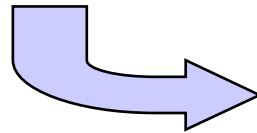
Proposed method

Consider electric field in the channel from source to drain :

$$\int_{source}^{drain} \mathbf{dx} \cdot \mathbf{E} = - \int_{source}^{drain} \nabla V - j\omega \int_{source}^{drain} \mathbf{dx} \cdot \mathbf{A}$$



$$V_{ds} = \int_{source}^{drain} \mathbf{dx} \cdot \mathbf{E} - j\omega \int_{source}^{drain} \mathbf{dx} \cdot \mathbf{A}$$



$$V_{ds} + j\omega L_{ds} A_x(\mathbf{r}) = \int_{source}^{drain} \mathbf{dx} \cdot \mathbf{E}$$

An environment variable is found: $V_{ds}^{hook} = j\omega L_{ds} A_x(\mathbf{r})$

Refinements to the proposal

- ‘Subtle’ detail:
 - A constant vector potential can not generate a magnetic field

- **Zero order** approximation:

$$\mathbf{A}(\mathbf{r}) \cong \mathbf{A}(\mathbf{r}_0) \quad \Longrightarrow \quad \mathbf{B} = \mathbf{0}, \quad V = V + \frac{j\omega}{c} \int \mathbf{A} d\mathbf{r}$$

- **First order** approximation:

$$\mathbf{A}(\mathbf{r}) \cong \mathbf{A}(\mathbf{r}_0) + \left. \frac{d\mathbf{A}}{d\mathbf{r}} \right|_{\mathbf{r}_0} (\mathbf{r} - \mathbf{r}_0) \quad \Longrightarrow \quad \mathbf{B}(\mathbf{r}) = \nabla \times \mathbf{A} \quad \text{constant}$$

- **Higher order** approximation:

$$\mathbf{A}(\mathbf{r}) \cong \mathbf{A}(\mathbf{r}_0) + \left. \frac{d\mathbf{A}}{d\mathbf{r}} \right|_{\mathbf{r}_0} (\mathbf{r} - \mathbf{r}_0) + \dots \quad \Longrightarrow \quad \mathbf{B}(\mathbf{r}) = \nabla \times \mathbf{A}$$

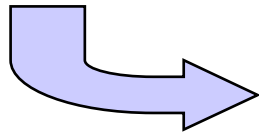
- Model refinement:
 - In order to include the effect of magnetic induction in active devices a linearly-varying vector potential must be taken

$$B_i = \epsilon_{ijk} \frac{\partial A_j}{\partial x_k}$$

Model refinement

- When are magnetic fields important ?
 - If the Lorentz force law matters

$$\mathbf{E} \rightarrow \mathbf{E} + \mathbf{v} \times \mathbf{B}$$



$$\mathbf{J} = \sigma \left(\mathbf{E} + \frac{\mathbf{J}}{q\rho} \times \mathbf{B} \right) = \sigma \mathbf{E} + \mu \mathbf{J} \times \mathbf{B}$$

metal

$$\mathbf{J}_p = \mu_p q p \mathbf{E} - q D_p \nabla p + q p \mathbf{v}_p \times \mathbf{B}$$

$$\mathbf{J}_n = \mu_n q n \mathbf{E} + q D_n \nabla n - q n \mathbf{v}_n \times \mathbf{B}$$

$$\mathbf{v}_p = \frac{\mathbf{J}_p}{q p}$$

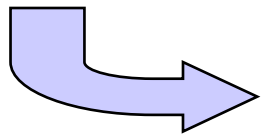
$$\mathbf{v}_n = -\frac{\mathbf{J}_n}{q n}$$

} semiconductor

Model refinements

- Solve the implicitly given currents

$$\begin{bmatrix} 1 & -\mu B_z & \mu B_y \\ \mu B_z & 1 & \mu B_x \\ -\mu B_y & \mu B_x & 1 \end{bmatrix} \begin{bmatrix} J_x \\ J_y \\ J_z \end{bmatrix} = \begin{bmatrix} \sigma E_x \\ \sigma E_y \\ \sigma E_z \end{bmatrix}$$

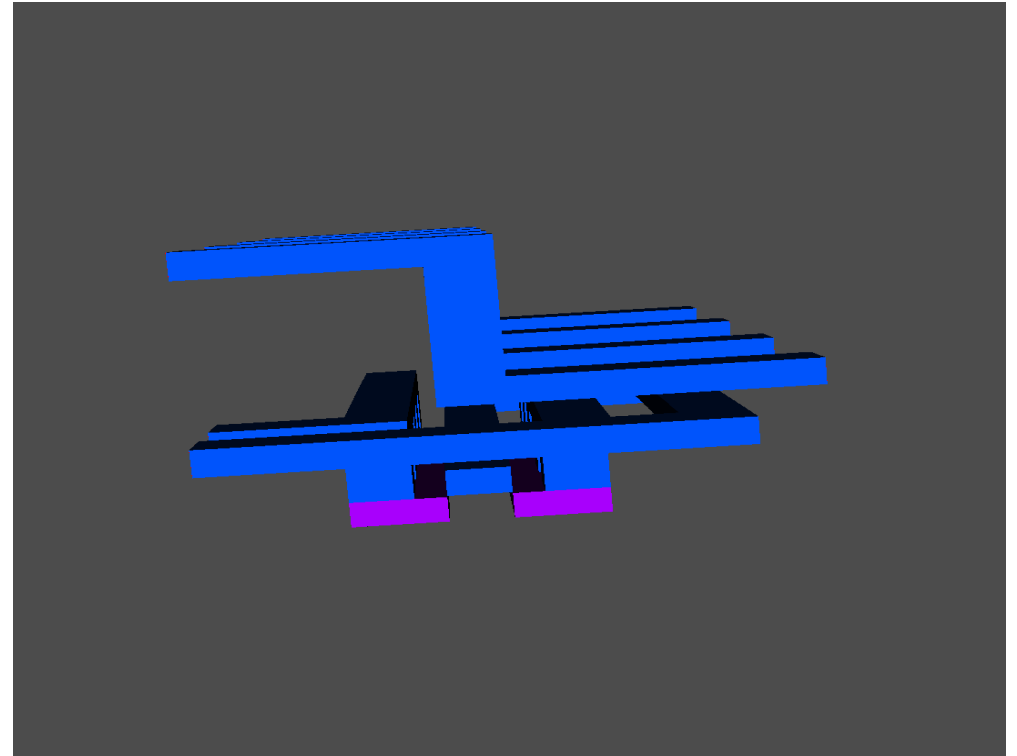
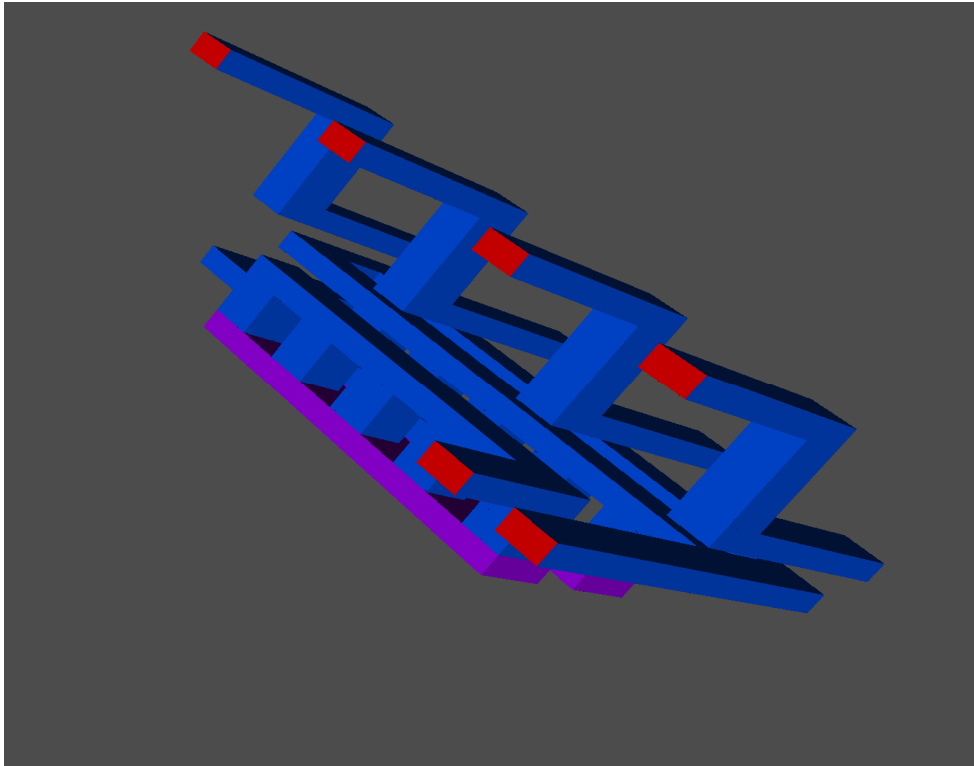


$$\mathbf{J} = \frac{1}{1 + \mu^2 B^2} \left(\sigma \mathbf{E} + \mu \sigma \mathbf{E} \times \mathbf{B} + \mu^2 \sigma (\mathbf{E} \cdot \mathbf{B}) \mathbf{B} \right)$$

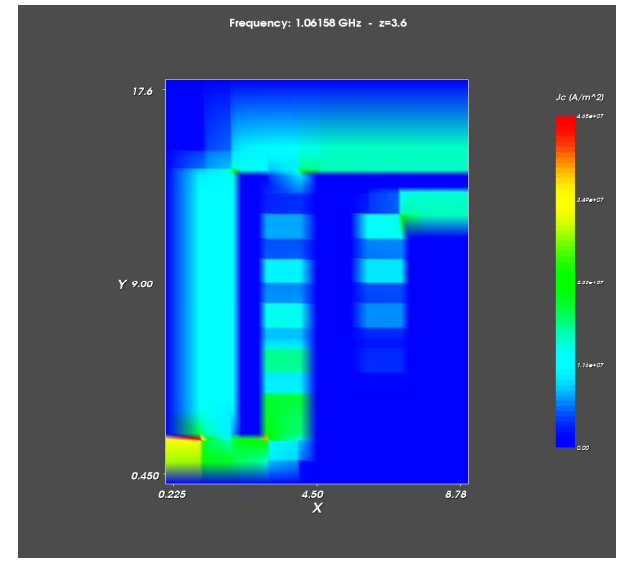
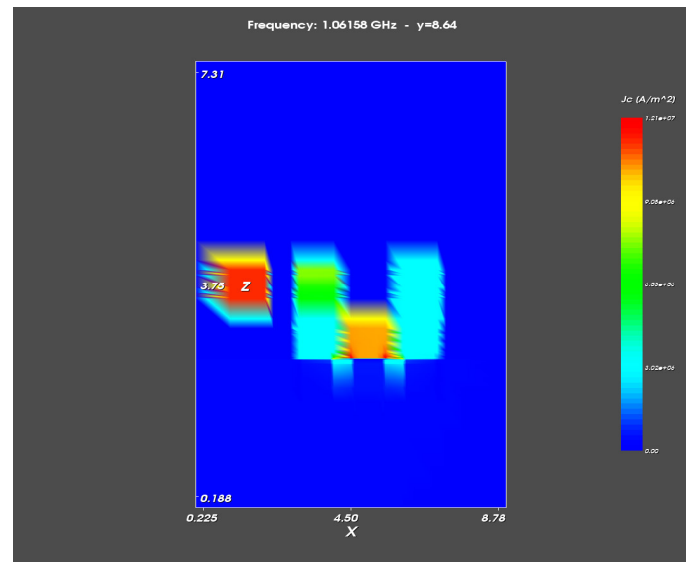
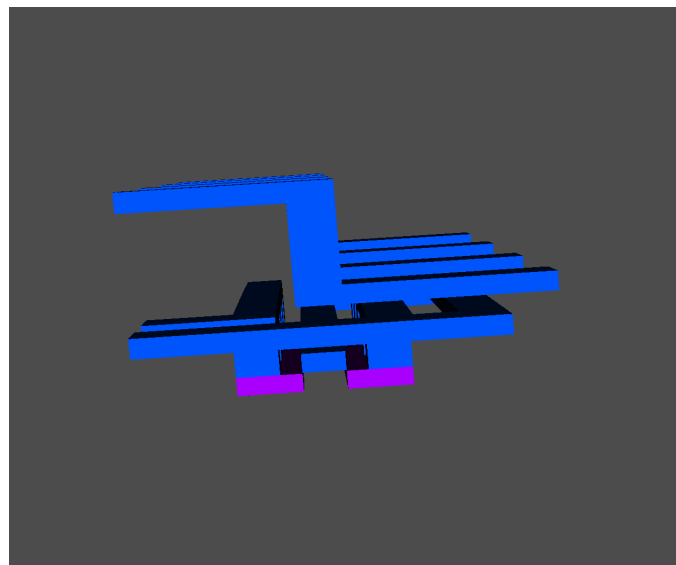
$$\mu B \ll 1 \quad \longrightarrow \quad \mathbf{J} = \sigma (\mathbf{E} + \mu \mathbf{E} \times \mathbf{B})$$

- This equation can be used to explore influence of \mathbf{B}

Calculate s-parameters of transistor and attached interconnect at once

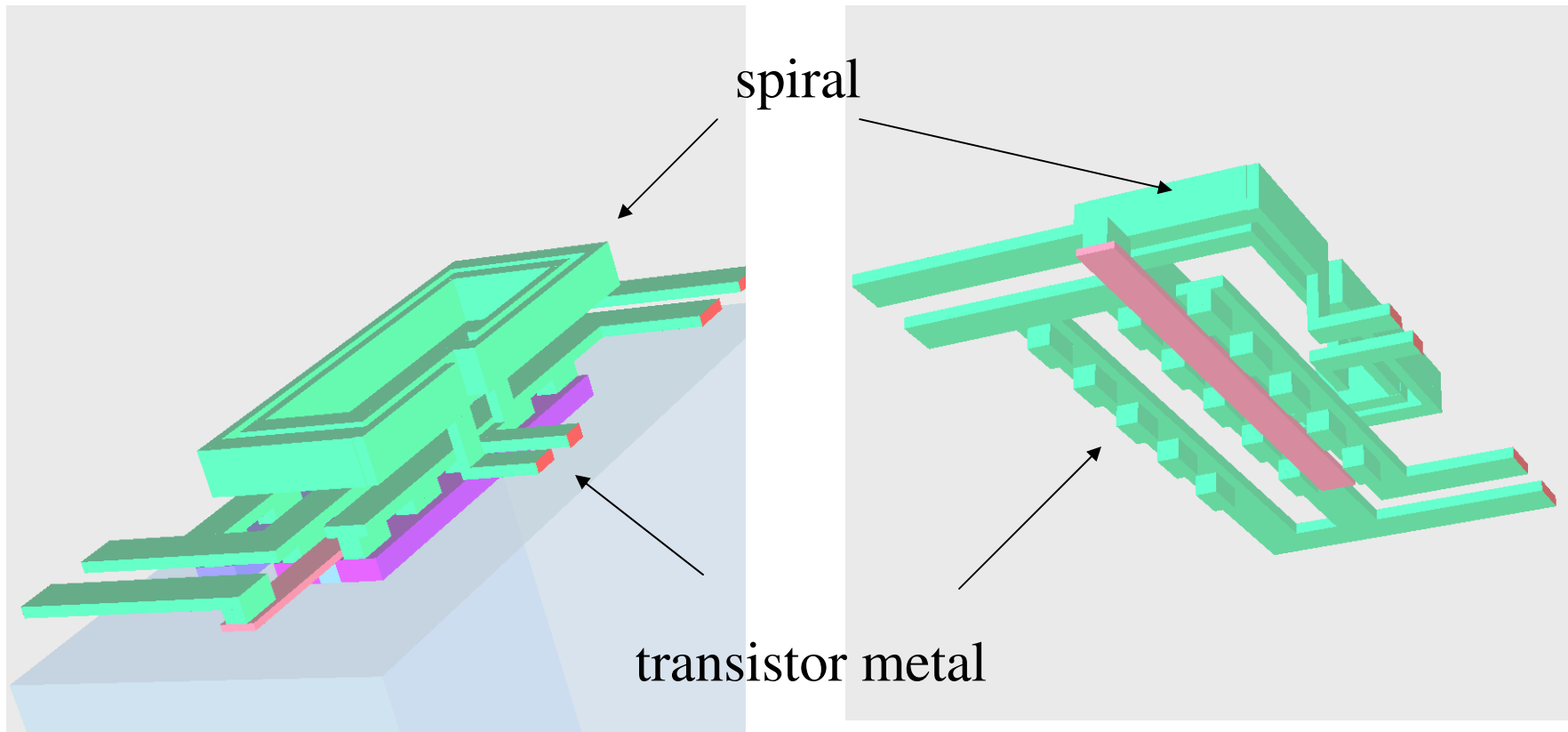


Visual inspection of currents in structure



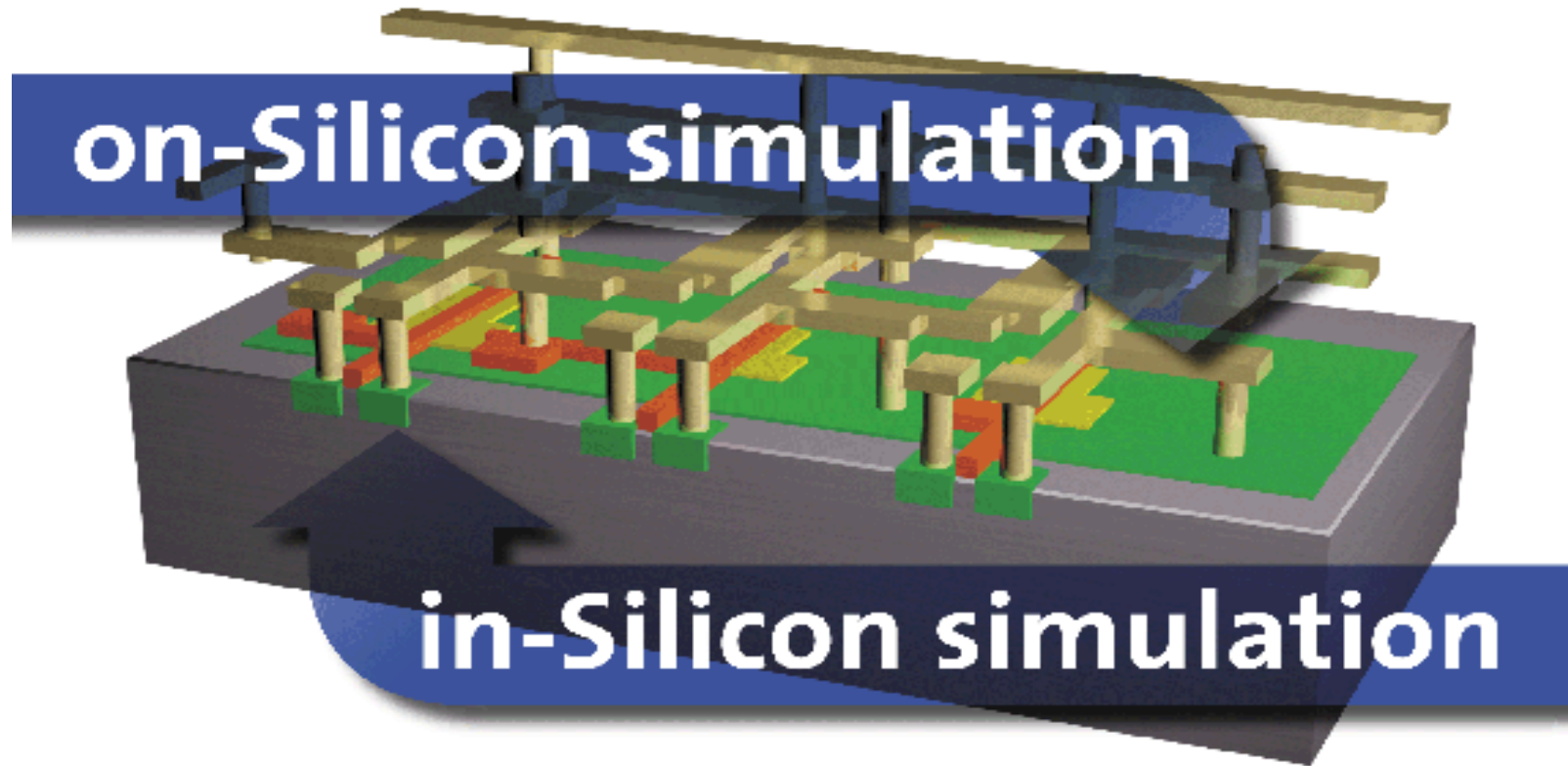
Second case under study

- Local inductor above the transistor



- An on set is made to view that devices are not only controlled by their port conditions, but:
- Generic injections are translated to port conditions
- Simulation studies can be performed by tools by which fields from in-chip ‘aggressor’ passives can be injected into ‘victim’ devices
- For further details see: www.magwel.com

Thank You !



Support from EU is gratefully acknowledged:
Codestar, nanoCMOS, Chameleon-RF, PULLNANO